

Study of the hygro-elastic behaviour of composite materials in presence of cracks: application to the durability of renewable marine energy structures

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Context

Problem

Composite structures submitted to **harsh environment**



Tidal turbines



Offshore windmill

Complex **coupled** loadings

- **Humidity**
- Temperature
- Chemical aggressions
- Solar radiations
- **Mechanical loadings**

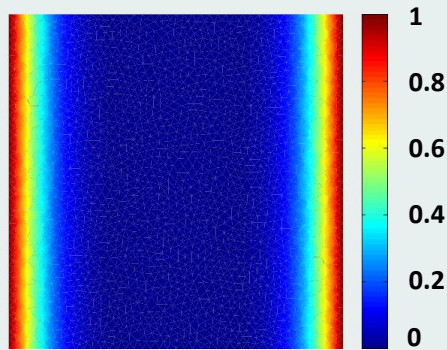
Impact of diffusion and mechanical loadings

- **Decrease** of the **mechanical properties** of the material
- Appearance of a **hygroscopic differential swelling** leading to **high stresses**
- Consequences: **cracks propagation**, delamination, fibre/matrix decohesion

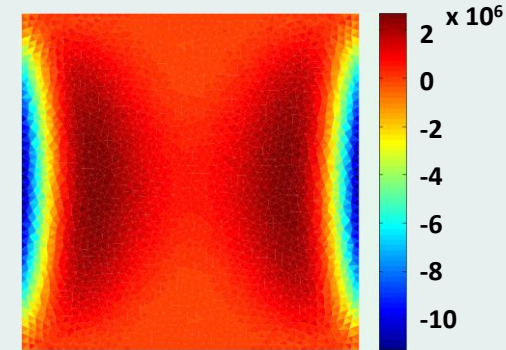
Interaction between moisture diffusion and mechanical behaviour

Hygroscopic swelling

The moisture content leads to a so-called **hygroscopic swelling** involving relevant **internal stresses**

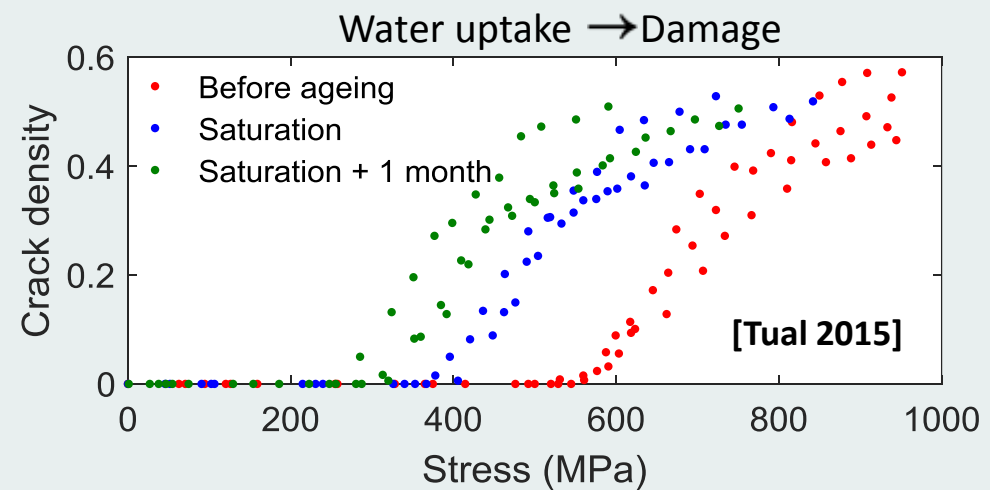
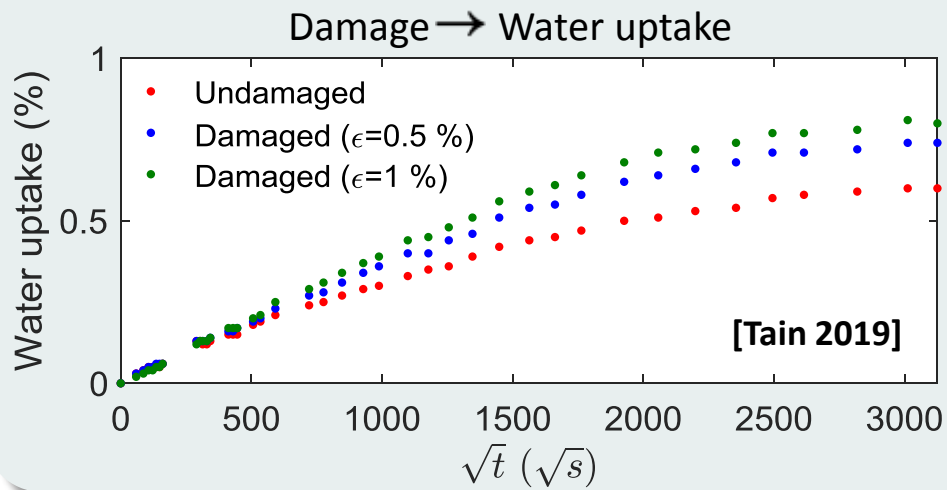


Local moisture content



Local stress field σ_{22} (Pa)

Mechanical properties and material damage



FIRMAIN project

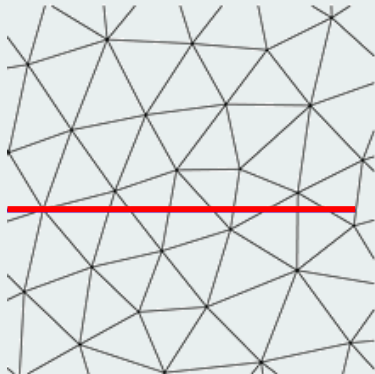
Impact of hygroscopic ageing on the cracking of composite materials in an uncertain context

- Development of relevant physical models
- Implementation of reliable numerical models
- Consideration of the sources of uncertainty

Development of reliable numerical methods combined with multi-physical models for the design of composite structures used as renewable marine energy conversion systems

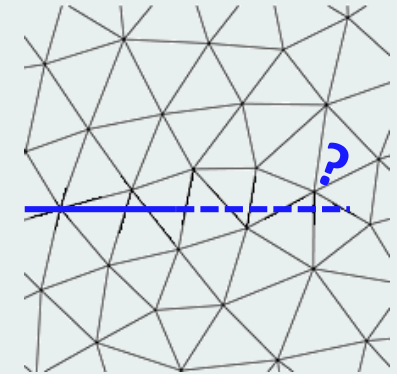
Numerical tools

X-FEM (Extended FEM)



- Does not require a conformed mesh
- Eases the study of crack propagation
- Takes into account the uncertainties
- Allows to study geometric variability

S-FEM (Stochastic FEM)

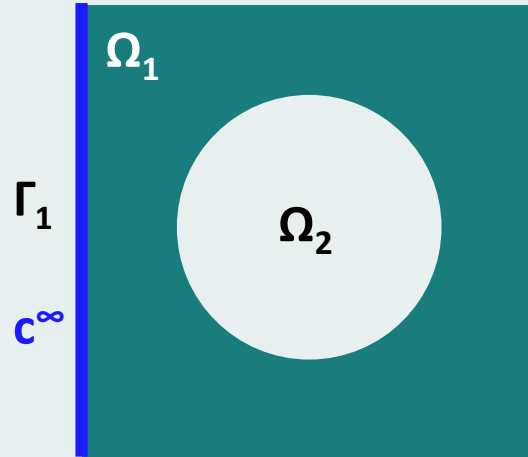


Outline

- Motivations
- Modelling and numerical approach
- X-FEM validation
- Numerical study : homogeneous case
- Numerical study : heterogeneous case
- Conclusions and future works

Fick diffusion model

Heterogeneous Fick problem : strong form



Find $c(\mathbf{x}, t) \in \Omega \times \mathbb{R}_*^+$ such that

$$\frac{\partial c(\mathbf{x}, t)}{\partial t} = \mathbf{D} \Delta c(\mathbf{x}, t) \quad \text{in} \quad \Omega \times \mathbb{R}_*^+$$

$$c(\mathbf{x}, t) = c^\infty \quad \text{on} \quad \Gamma_1 \times \mathbb{R}_*^+$$

$$(\mathbf{D} \nabla_{\mathbf{x}} c(\mathbf{x}, t)) \cdot \mathbf{n} = \mathbf{0} \quad \text{on} \quad \Gamma \setminus \Gamma_1 \times \mathbb{R}_*^+$$

$$c(\mathbf{x}, t = 0) = c_0(\mathbf{x}) \quad \forall \mathbf{x} \in \Omega$$

where $\Omega = \Omega_1 \cup \Omega_2$ and $\mathbf{D} = \begin{cases} \mathbf{D}_1 & \text{if } \mathbf{x} \in \Omega_1 \\ \mathbf{0} & \text{if } \mathbf{x} \in \Omega_2 \end{cases}$

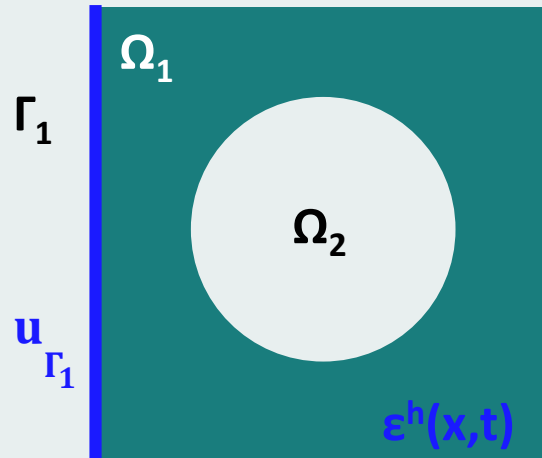
The spatial average water content $C(t)$ verifies :

$$C(t) = \frac{1}{M_0} \int_{\Omega} \rho(\mathbf{x}) c(\mathbf{x}, t) d\Omega$$

\mathbf{D} : diffusion coefficient
 c^∞ : saturation content

Mechanical problem model

Heterogeneous uncoupled hygro-elastic problem : strong form



Find $\mathbf{u}(\mathbf{x}, t) \in \Omega \times (0, T)$ such that

$$\operatorname{div} \boldsymbol{\sigma} + \mathbf{f} = \mathbf{0} \quad \text{in} \quad \Omega \setminus \Gamma_{crack} \times (0, T)$$

$$\boldsymbol{\sigma} = \mathbf{C} : (\boldsymbol{\varepsilon}(\mathbf{u}) - \boldsymbol{\varepsilon}^h(\mathbf{x}, t)) \quad \text{in} \quad \Omega \setminus \Gamma_{crack} \times (0, T)$$

$$\boldsymbol{\sigma} \cdot \mathbf{n} = \mathbf{0} \quad \text{on} \quad \Gamma \setminus \Gamma_{crack} \times (0, T)$$

$$\mathbf{u} = \mathbf{u}_{imp} \quad \text{on} \quad \Gamma_u \times (0, T)$$

where $\Omega = \Omega_1 \cup \Omega_2$ and $\mathbf{C} = \begin{cases} \mathbf{C}_1 & \text{if } \mathbf{x} \in \Omega_1 \\ \mathbf{C}_2 & \text{if } \mathbf{x} \in \Omega_2 \end{cases}$

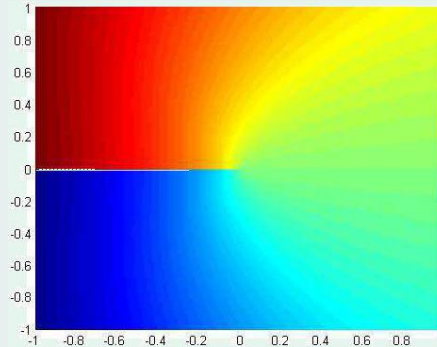
with $\boldsymbol{\varepsilon}^h(\mathbf{x}, t) = \begin{bmatrix} \beta_x^h c(\mathbf{x}, t) & 0 & 0 \\ \text{sym} & \beta_y^h c(\mathbf{x}, t) & 0 \\ & & \beta_z^h c(\mathbf{x}, t) \end{bmatrix}$

→ Field $c(\mathbf{x}, t)$ can be obtained from the Fick diffusion model

X-FEM methodology for hygro-mechanical problems

Main ingredients of the X-FEM approach

- Implicit description of the geometry with the **level-sets** techniques [Sethian 1999]



- **Enriched approximation** based on the level-set function to **capture irregularities** in the solution field [Moës et al. 1999]

Specificities implemented for the hygro-mechanical problem

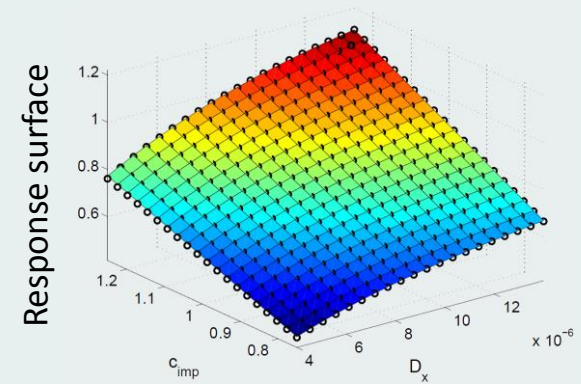
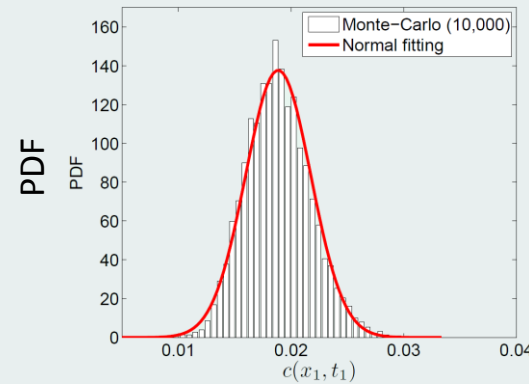
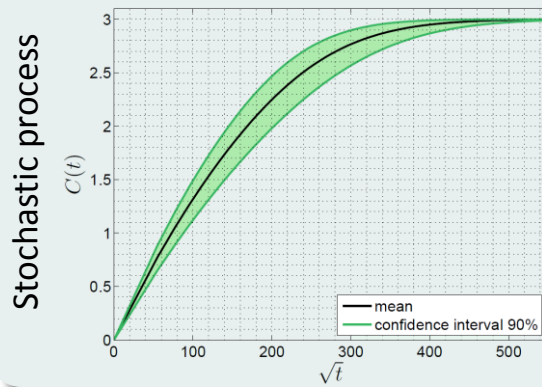
- **Penalty approach** for imposing Dirichlet **boundary conditions** on interfaces modeled with level-sets [Fernandez et al. 2004]
- Computation of the hygroscopic strains: find $u \in \mathcal{W}(v)$ such as

$$\int_{\Omega \setminus \Gamma_{crack}} \varepsilon(v) : \mathbf{C} : \varepsilon(u) d\Omega = \int_{\Omega \setminus \Gamma_{crack}} \varepsilon(v) : \mathbf{C} : \varepsilon^h d\Omega$$

Spectral stochastic approach for uncertainties propagation

Objectives of the approach

Computation of the **output variability** with respect to the **input uncertainties**



Decomposition of the solution on a specific basis suited the stochastic problem

The discrete solution $c(\mathbf{y}, \xi)$ will be searched under the form

$$c(\mathbf{y}, \xi) \approx \sum_{\alpha=1}^P c_{\alpha}(\mathbf{y}) H_{\alpha}(\xi)$$

where the $c_{\alpha}(\mathbf{y})$ are the unknown of the problem and the $\{H_{\alpha}\}_{\alpha=1}^P \in L^2(\Xi, dP_{\xi})$ is a basis of orthonormal polynomials choosing with respect to the density of probability P_{Ξ} (**Polynomial Chaos** [Ghanem et al. 1991, Xiu et al. 2002])

→ computation of the unknown with a **non-intrusive L^2 projection method** which only requires deterministic computations for particular realizations of ξ [Le Maître et al. 2010]

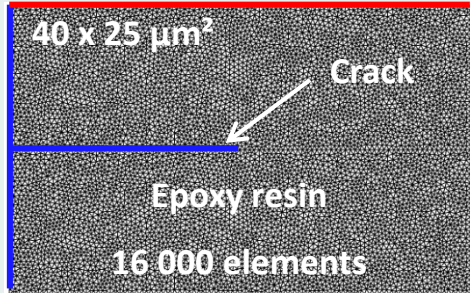
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X-FEM / FEM comparison

Model

Mechanical loading $\sigma = 1.5 \text{ MPa}$



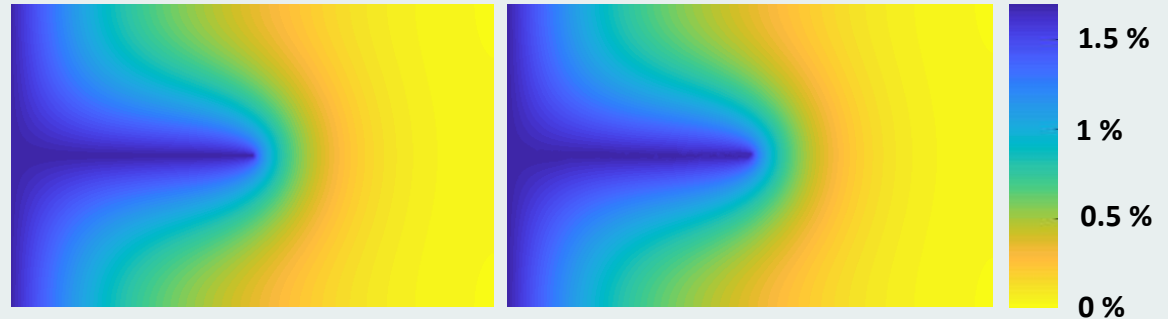
$E = 4 \text{ GPa}$
 $\nu = 0.36$
 $\rho = 1310 \text{ kg/m}^3$
 $\beta = 0.324 \%$

Hygroscopic loading : $c^\infty = 1.71 \%$

$D = 8.2e-2 \mu\text{m}^2/\text{s}$

Water diffusion

Comparison of water uptake at a specific time ($t=500 \text{ s}$)

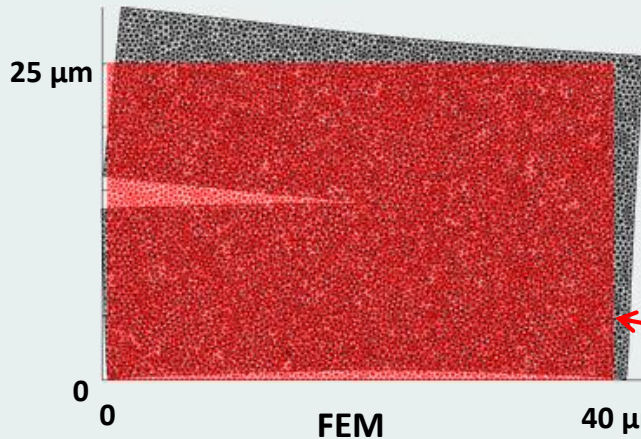


FEM

X-FEM

Displacement field

Mechanical + hygroscopic loading ($t=500 \text{ s}$)

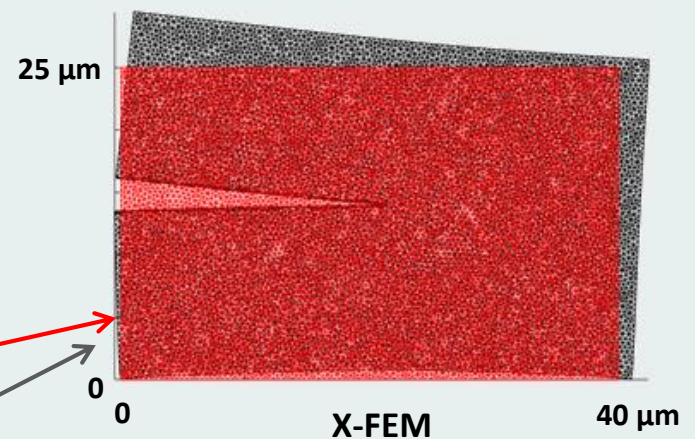


FEM

Initial undeformed shape

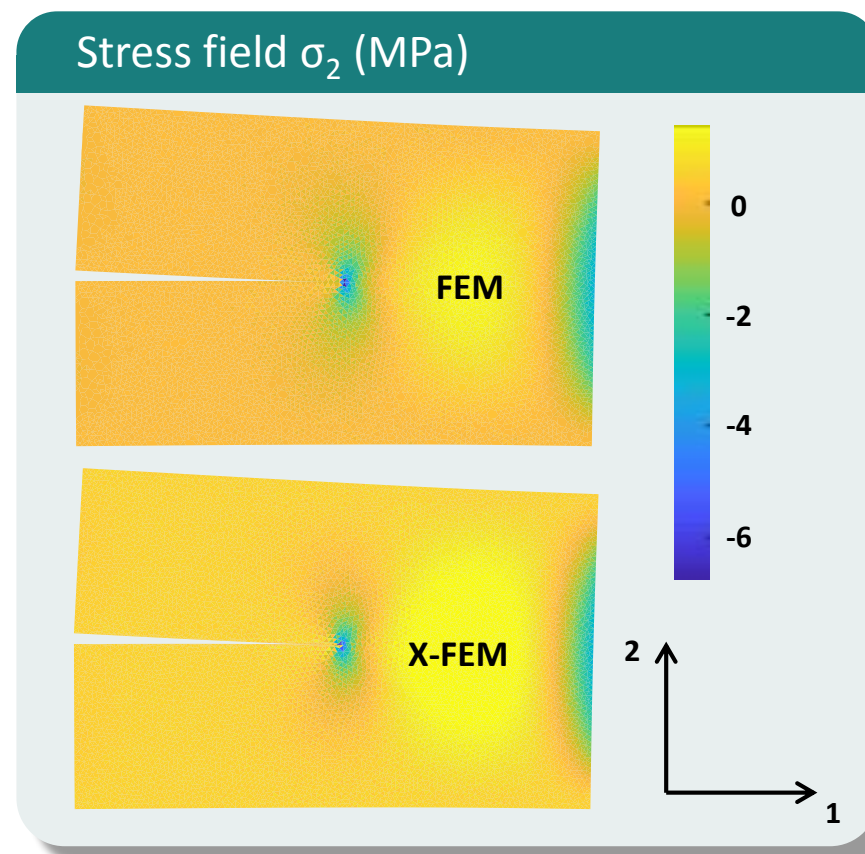
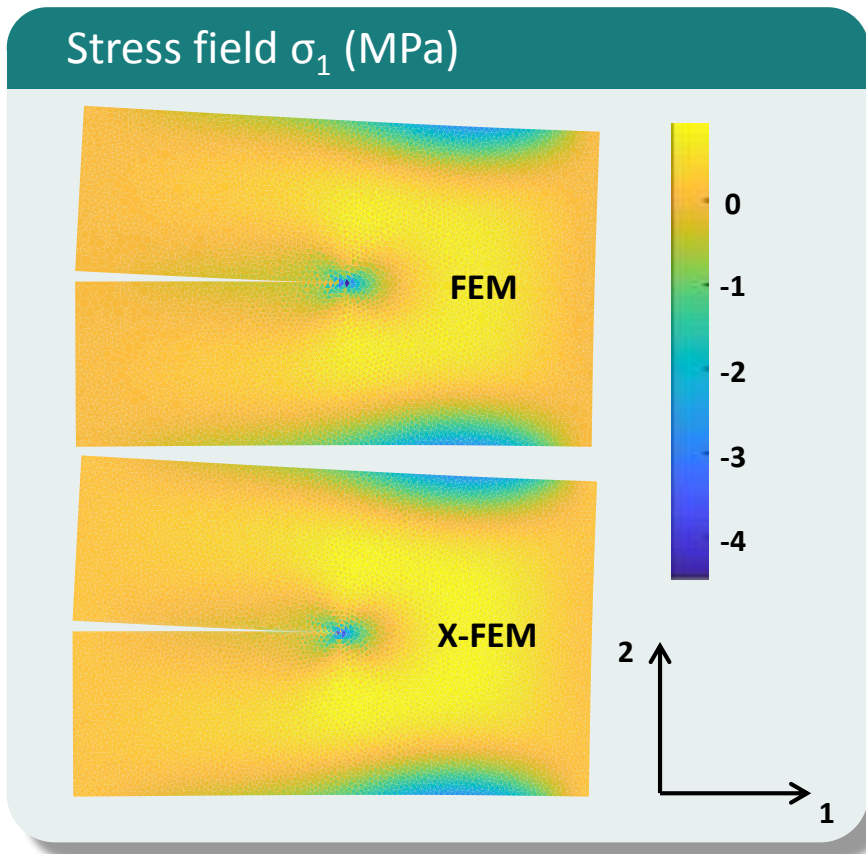
Final deformed shape

Mechanical + hygroscopic loading ($t=500 \text{ s}$)



X-FEM

X-FEM / FEM comparison



Conclusion

✓ Validation of X-FEM model ✓

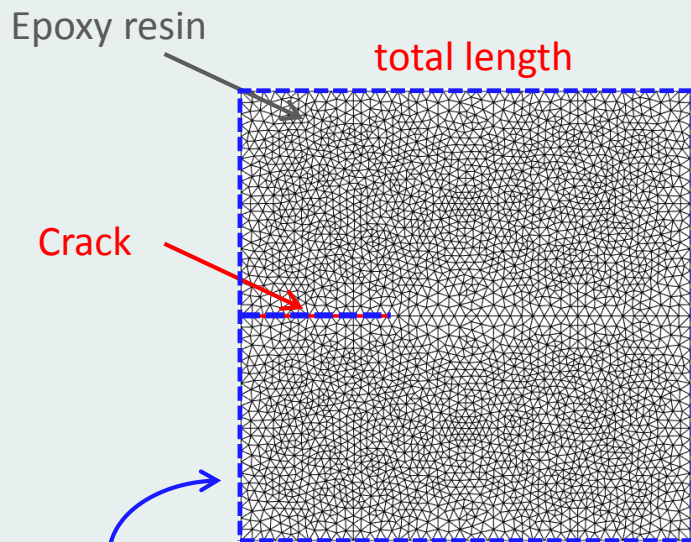
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Effect of cracking on diffusion – homogeneous case

Meshing and boundary conditions

Cracking ratio $r = \frac{\text{crack length}}{\text{total length}}$

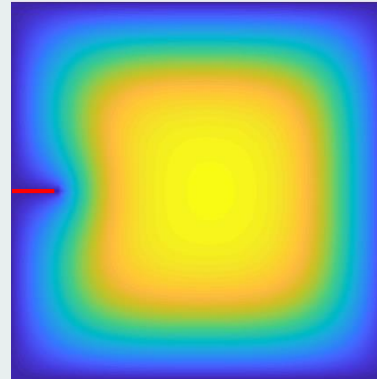


$c^\infty = 1,71\%$
48 x 48 μm^2

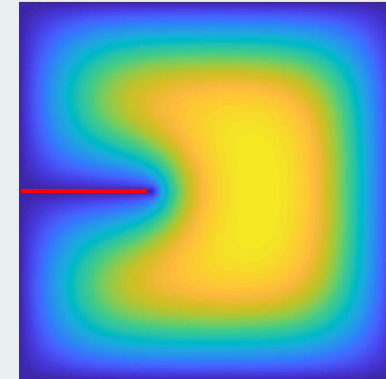
3500 elements

Diffusion versus cracking ratio

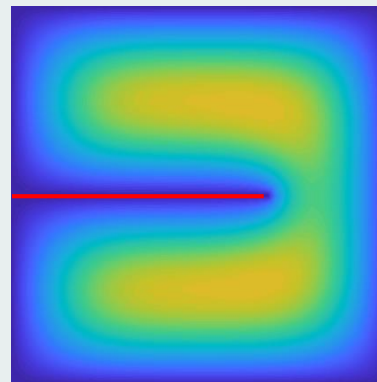
$r = 1/9$



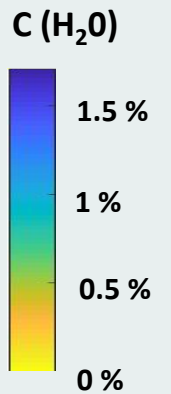
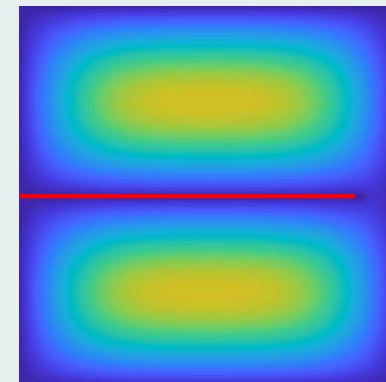
$r = 3/9$



$r = 6/9$

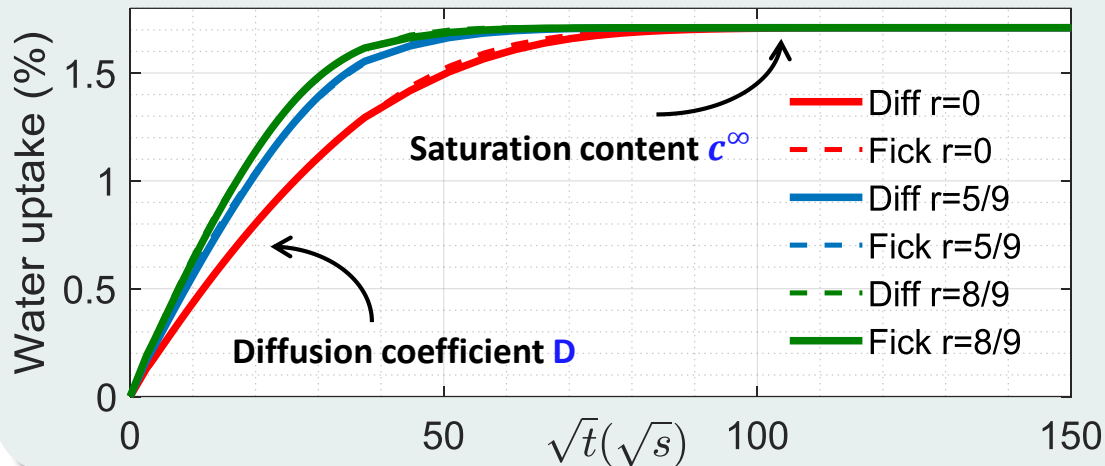


$r = 8/9$

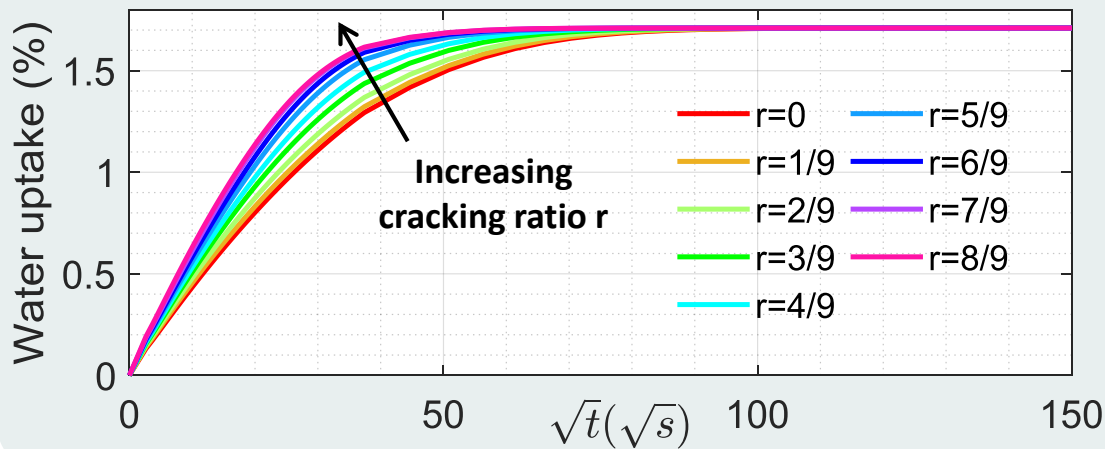


Effect of cracking on diffusion – homogeneous case

Identification of diffusion curves using a Fick model

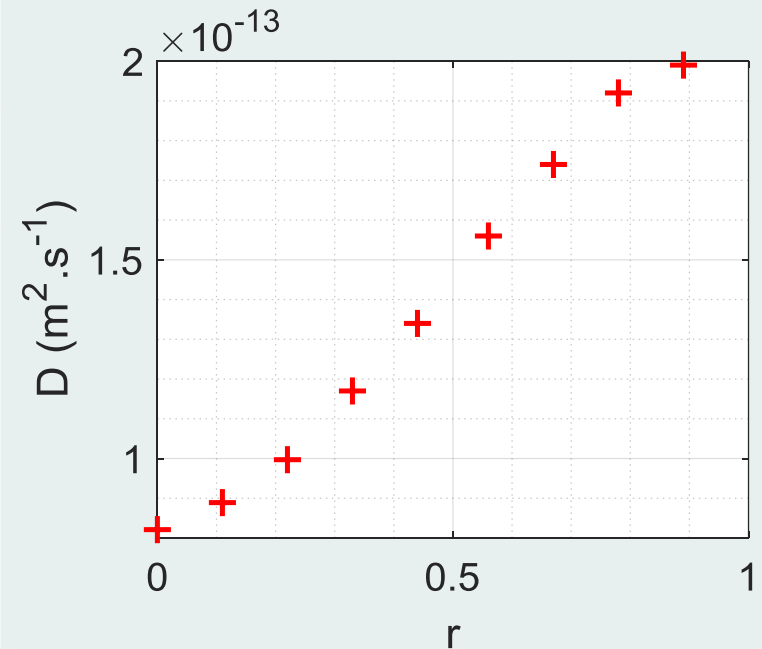


Evolution of diffusion curves as a function of r



Conclusions

- Accurate identification of the diffusion curves
- The larger the crack size, the faster the diffusion occurs



- **Non-linear evolution** of $D = f(r)$

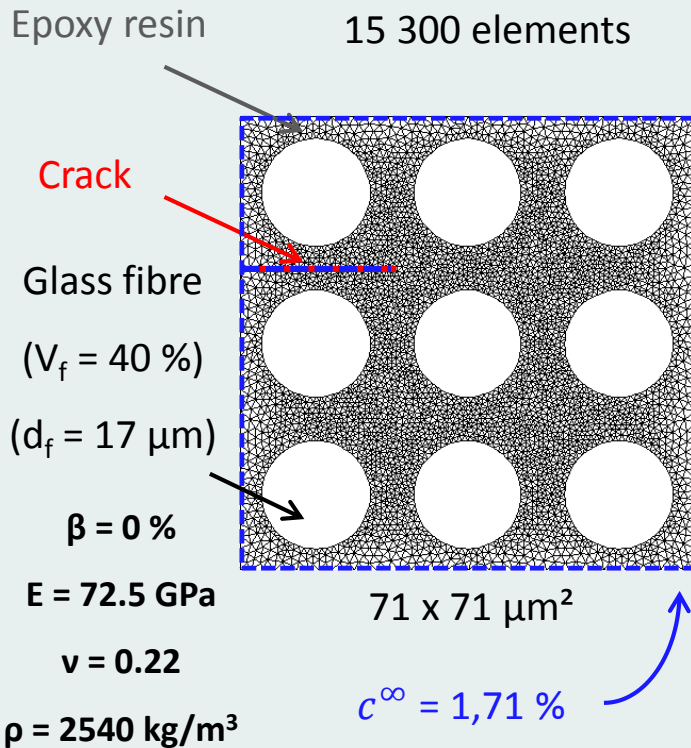
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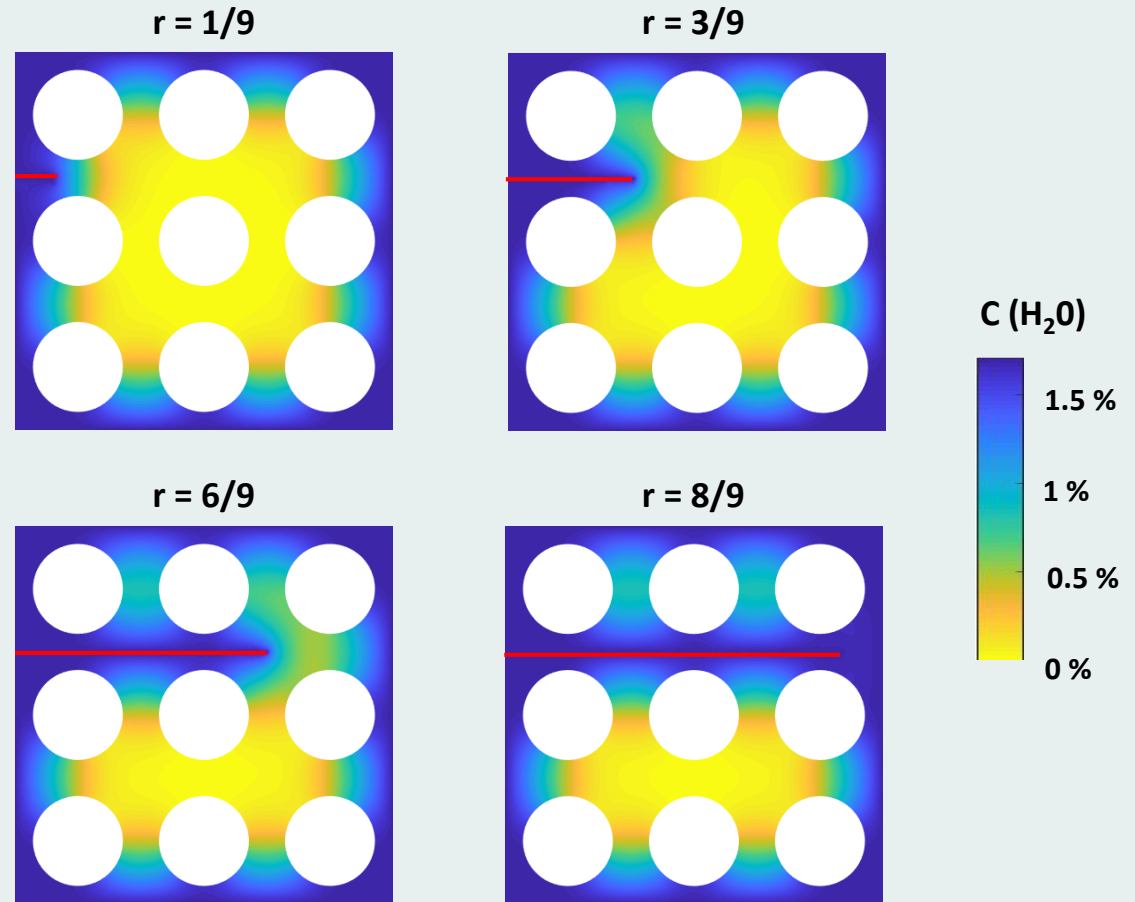
Effect of cracking on diffusion – heterogeneous case

Meshing and boundary conditions

Cracking ratio $r = \frac{\text{crack length}}{\text{total length}}$

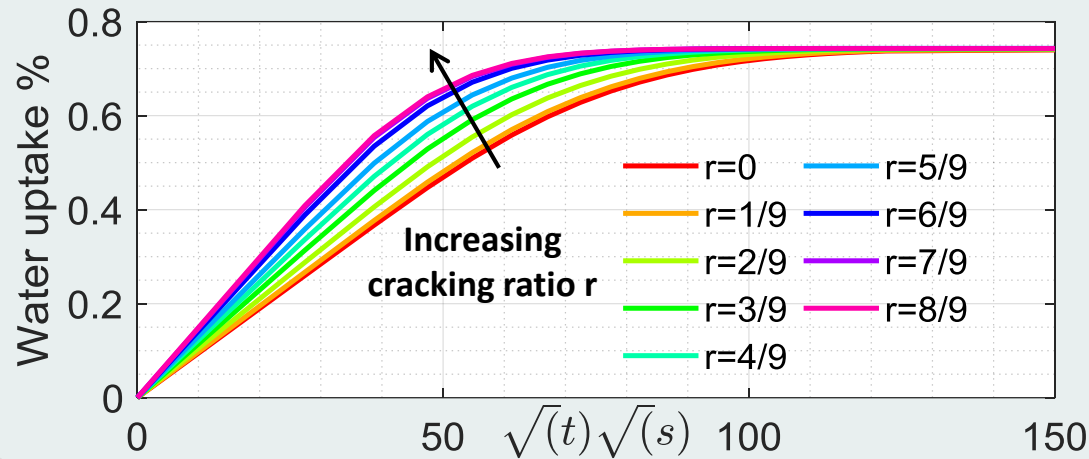


Diffusion versus cracking ratio

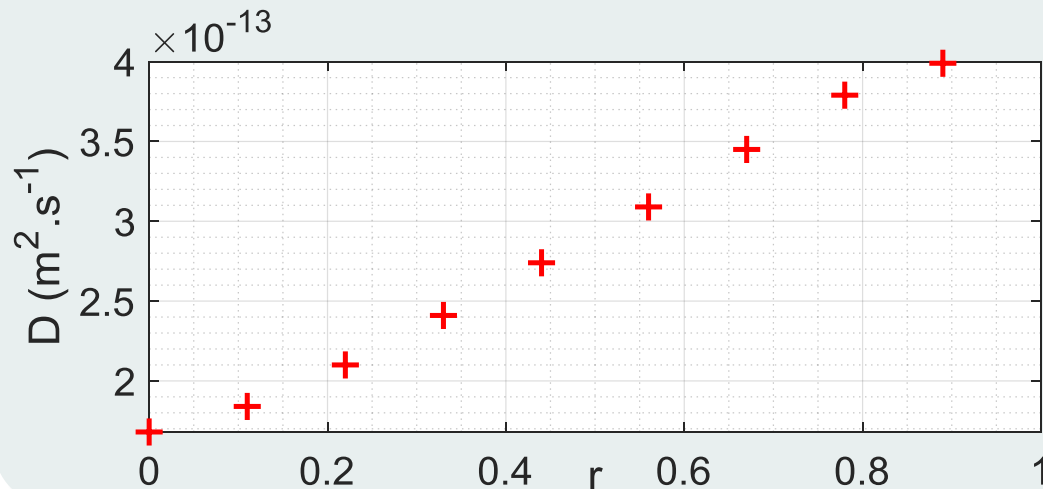


Effect of cracking on diffusion – heterogeneous case

Evolution of diffusion curves as a function of r



Evolution of diffusion coefficient as a function of r



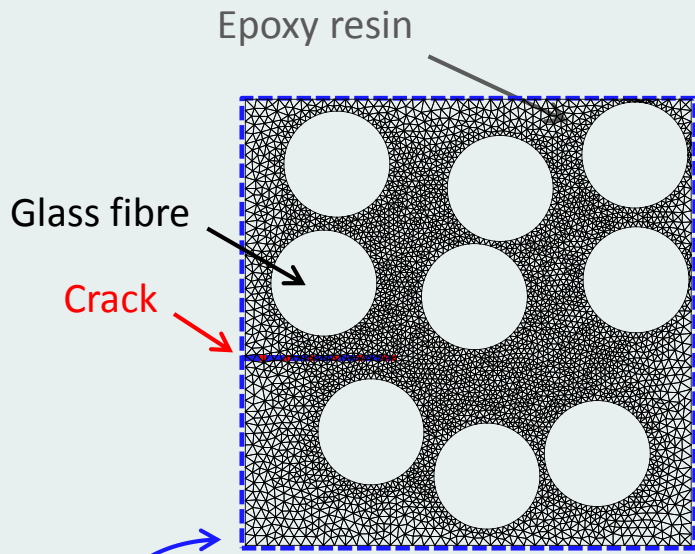
Conclusions

- Accurate identification of the diffusion curves
- The larger the crack size, the faster the diffusion occurs
- Saturation content is only 0.75 % (whereas $c_{imp}=1.71$ %) because fibers are not subjected to water uptake
- **Non-linear evolution** of $D = f(r)$

Effect of cracking on diffusion – heterogeneous random case

Meshing and boundary conditions

Cracking ratio $r = \frac{\text{crack length}}{\text{total length}}$



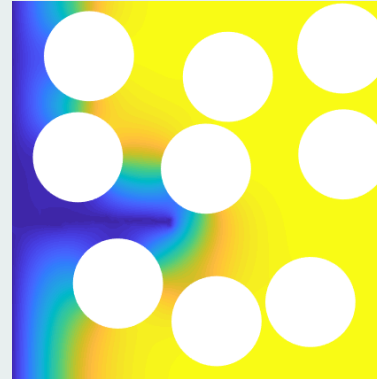
71 x 71 μm^2

$c^\infty = 1,71\%$

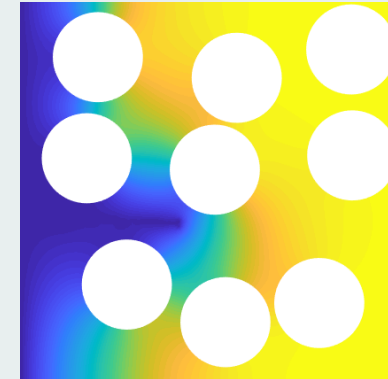
14 900 elements

Diffusion over time ($r=0.42$)

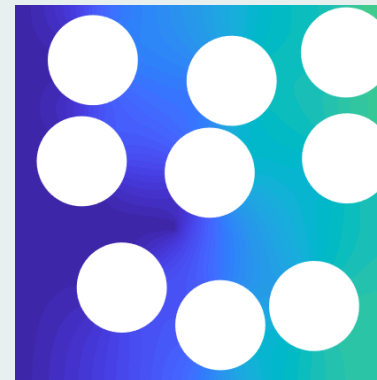
t = 0,2 h



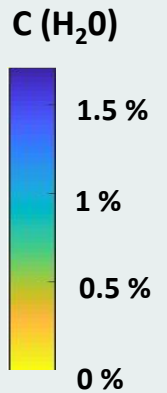
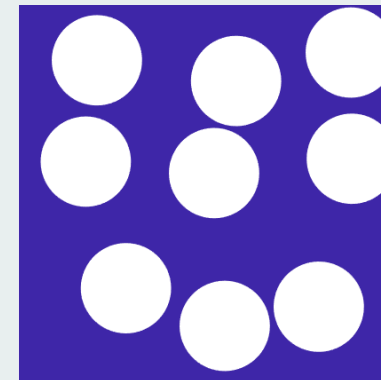
t = 0,5 h



t = 5 h

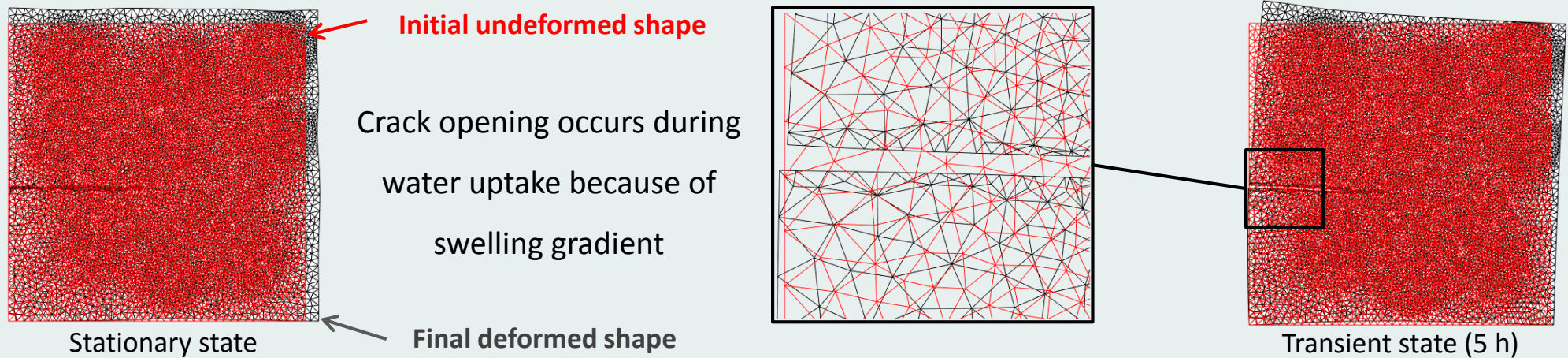


t = 27 h

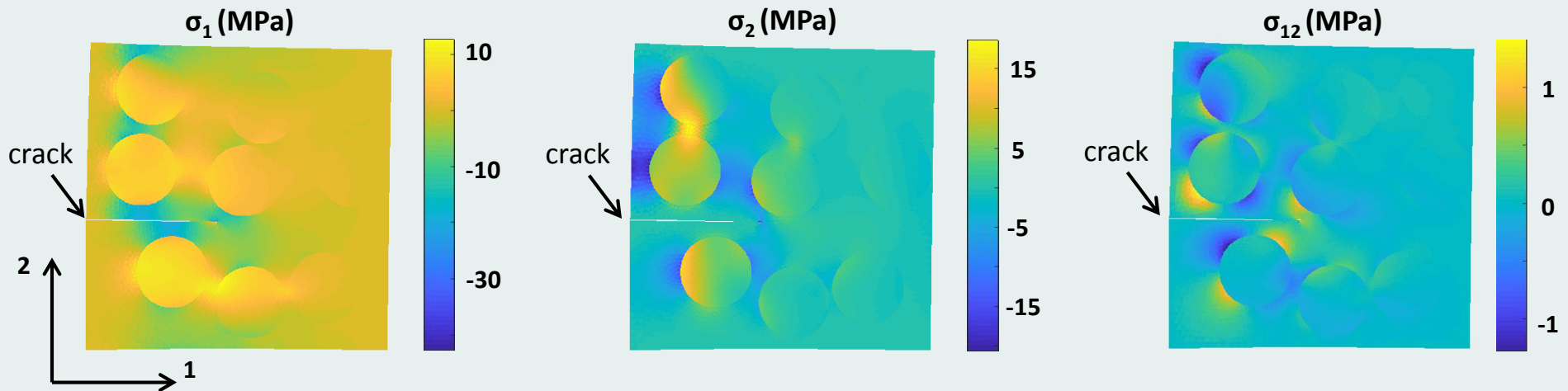


Effect of cracking on diffusion – heterogeneous random case

Hygroscopic strain fields during diffusion



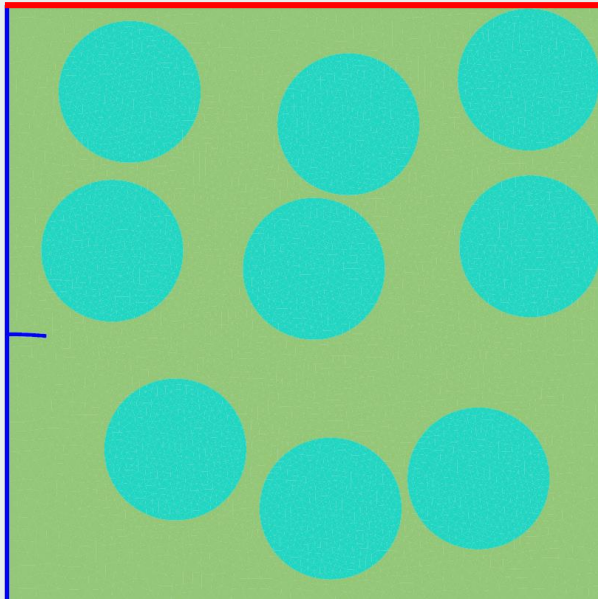
Hygroscopic stress fields during diffusion (transient state - 5 h)



Internal stresses and opening of the crack appear because of the swelling gradient during diffusion

Stochastic numerical study

Problem diffusion



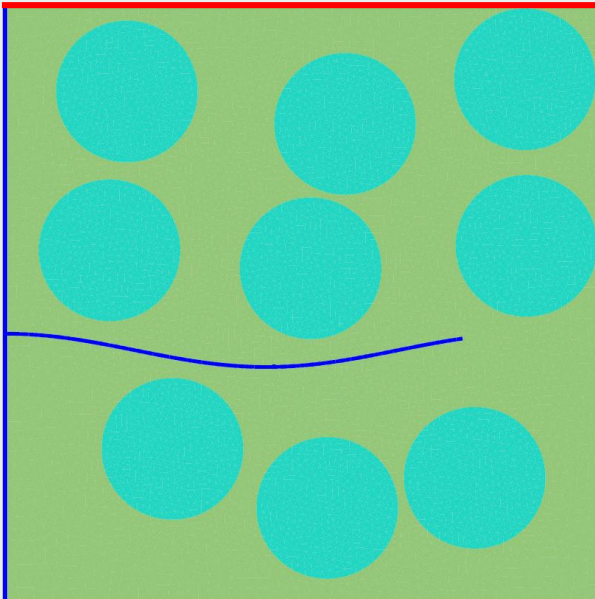
- Random crack length $L_{\text{crack}} \in (5, 55) \mu\text{m}$ (cov = 50 %)
- Random imposed $C_{\infty} \in (1.6, 1.8) \% H_2O$ (cov = 4 %)
- **Mechanical loading** $\sigma = 1.5 \text{ MPa}$ imposed on the top edge
- Isotropic moisture diffusion tensor with $D = 8.2 \cdot 10^{-2} \mu\text{m}^2/\text{s}$
- Volume fraction $v_f = 40 \%$ with $d_f = 17 \mu\text{m}$
- Epoxy elastic parameters : $E_m = 4 \text{ GPa}$, $\nu_m = 0.36$ and $\beta = 0.324 \%$
- Glass elastic parameters : $E_f = 72.5 \text{ GPa}$, $\nu_f = 0.22$ and $\beta = 0 \%$

Approximation parameters

- Spatial approximation with 14000 linear finite elements
- Euler's implicit time scheme for $T = 45 \text{ h}$ with $\Delta t = 10 \text{ min}$
- Penalty parameter $\gamma = 10^6$
- Stochastic approximation based on **polynomial chaos with order $p = 3$**

Stochastic numerical study

Problem diffusion



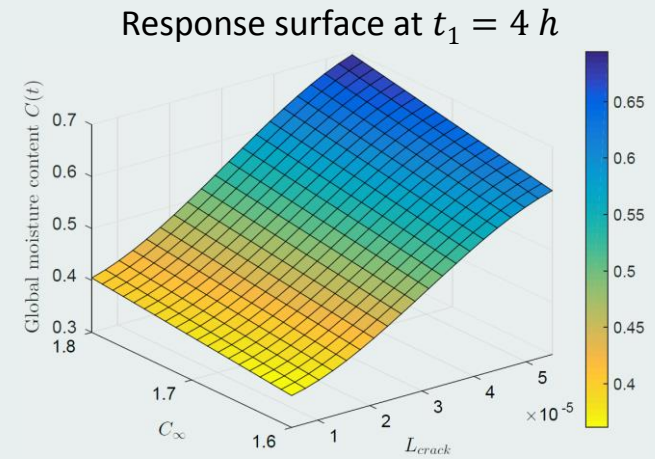
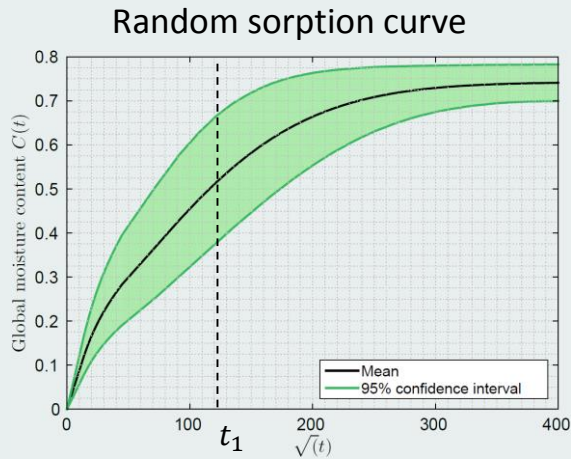
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Approximation parameters

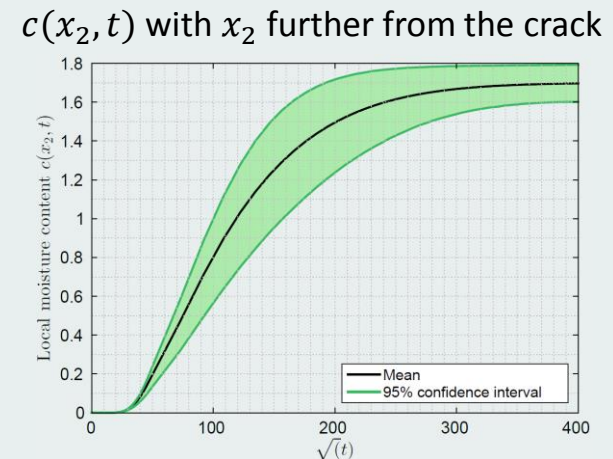
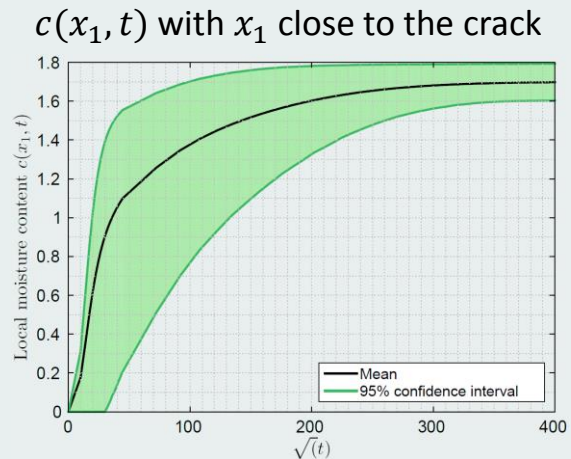
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Stochastic numerical study: diffusion results

Results on the global moisture content $C(t)$



Results on the local moisture content $c(x, t)$

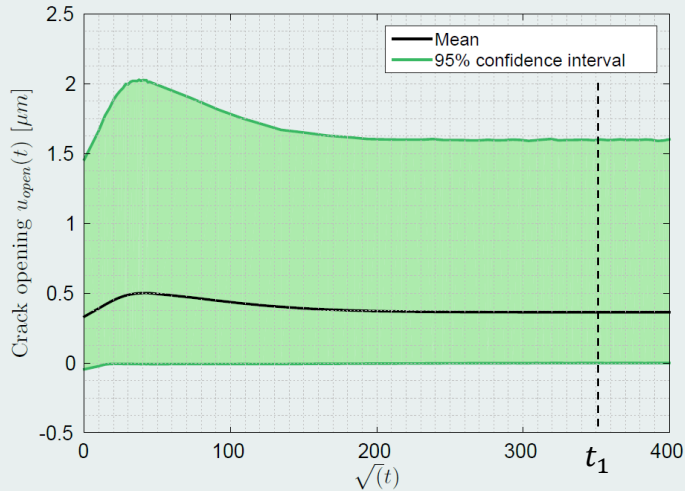


→ relevant influence of the crack length on both **global and local** moisture contents

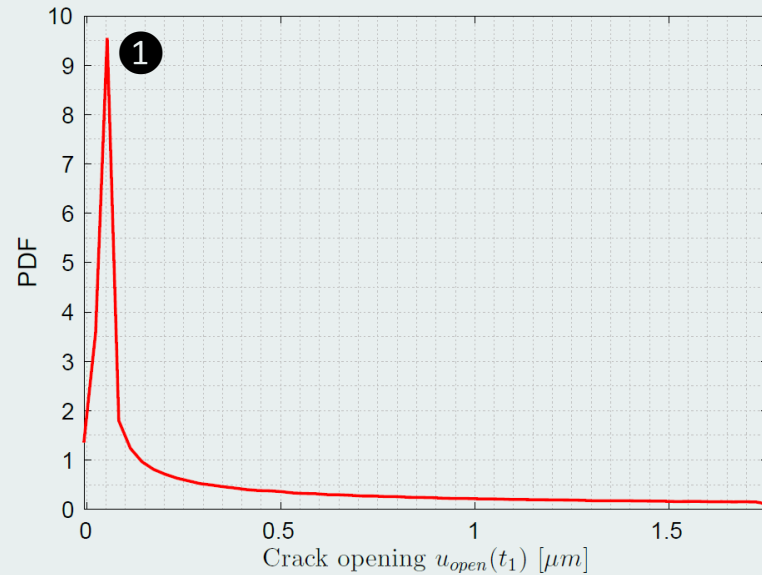
Stochastic numerical study: mechanical results

Results on the vertical crack opening $u_{open}(t)$

Stochastic process $u_{open}(t)$

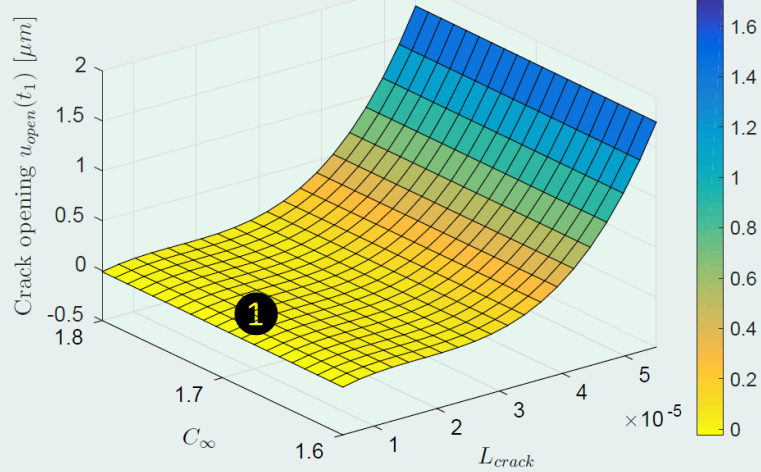


PDF at $t_1 = 35 h$



$$P(u_{open}(t_1) > 1.5 \mu m) = 4 \%$$

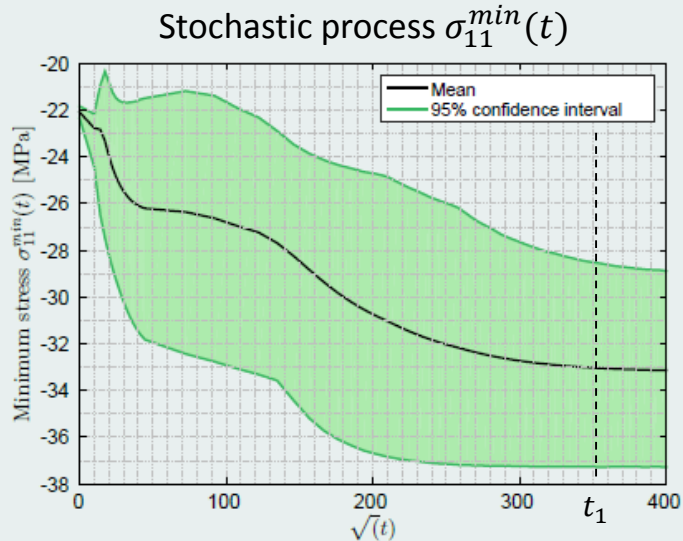
Response surface at $t_1 = 35 h$



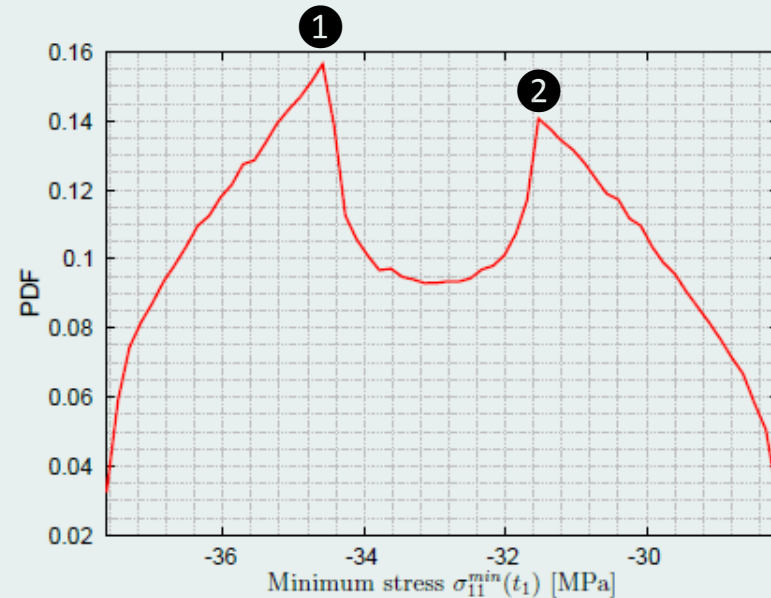
Significant variability mainly due to the crack length randomness

Stochastic numerical study: mechanical results

Results on the minimum local stress $\sigma_{11}^{min}(t)$ – compressive state

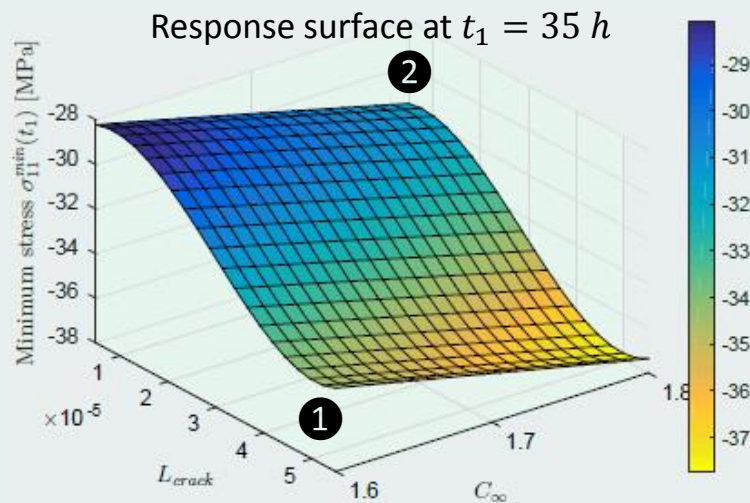


PDF at $t_1 = 35 h$



$$P(\sigma_{11}^{min}(t) \leq -37 \text{ MPa}) = 4.7 \%$$

Significant variability mainly due to the crack length randomness but also to the maximum absorption capacity randomness



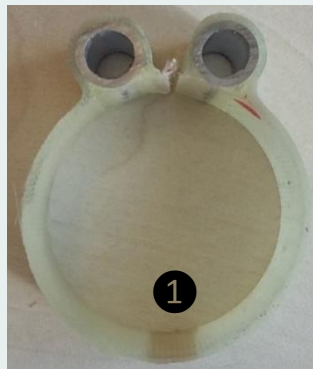
Conclusions & future works

Conclusions

- Study of the impact of **hygroscopic ageing on the cracking** of composite materials in a deterministic and stochastic context
- Implementation of numerical models based on **X-FEM** and **S-FEM** methods
- Consideration of **uncertainties** to study the influence of the geometric and diffusion parameters

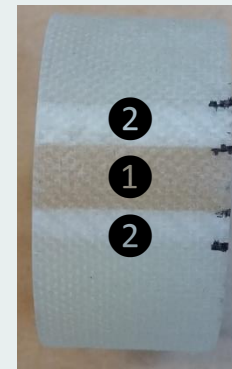
Ongoing and future works

- Dealing with the **random crack propagation** problem coupled with diffusion phenomenon (computation of stress intensity factors & numerical uptake of the level-set function during crack propagation)
- **Gathering experimental data** to obtain real input parameters and validate the numerical approach



① controlled defect

② defect propagation



Study of the hygro-elastic behaviour of composite materials in presence of cracks: application to the durability of renewable marine energy structures

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Thank you for your attention

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